

Roll No.

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Total No. of Questions: 09

Total No. of Pages: 02

B. Tech. (CE) (Sem. 6)
NUMERICAL METHODS IN CIVIL ENGINEERING
Subject Code: BTCE-604
Paper ID: A2291

Time: 03 Hrs.

Max. Marks: 60

INSTRUCTIONS TO CANDIDATES:

1. Section A is **COMPULSORY** consisting of **TEN** questions carrying **TWO** marks each.
2. Section B contains **FIVE** questions carrying **FIVE** marks each and students have to attempt any **FOUR** questions.
3. Section C contains **THREE** questions carrying **TEN** marks each and students have to attempt any **TWO** questions.

SECTION A

1.

- a) Write a short note on initial value problem.
- b) Find the Eigenvalues and Eigenvector of the matrix
- c) Write a short note on Galerkin's method of least square.
- d) Classify the equation

$$(1 + x^2) \frac{\partial^2 u}{\partial x^2} + (5 + 2x^2) \frac{\partial^2 u}{\partial x \partial t} + (4 + x^2) \frac{\partial^2 u}{\partial t^2} = 0.$$
- e) Evaluate $\Delta^n(e^x)$, the interval of differencing being unity.
- f) Find a second degree polynomial from the following data

x:	0	1	2
y:	1	6	17
- g) Using iterative method find the inverse of matrix

$$\begin{bmatrix} 1 & 10 \\ 2 & 0 \end{bmatrix}$$
- h) Find the general solution of the difference equation

$$\Delta^2 u_n - 3\Delta u_n + 2u_n = 0$$
- i) Find the interval on which the root of the equation $x^3 - 2x - 5 = 0$ lies.
- j) Write Newton Raphson formula for the solution of non-linear equation.

SECTION B

2. Solve the system by Jordan method
 $2x + y + z = 10$
 $3x + 2y + 3z = 18$
 $x + 4y + 9z = 16$
3. Solve the boundary value problem
 $\frac{d^2y}{dx^2} - y = 0$ with $y(0)=0$ and $y(2)=3.62686$
4. Find a real root of the equation $3x = \cos x + 1$.
5. Explain the New marks method for solving the non linear problems.
6. Fit a second degree polynomial to the following data

x:	1.0	1.5	2.0	2.5	3.0	3.5	4.0
y:	1.1	1.3	1.6	2.0	2.7	3.4	4.1

SECTION C

7. Using Runge Kutta method of fourth order, solve
 $\frac{dy}{dx} = \frac{y^2 - x^2}{y^2 + x^2}$ with $y(0)=1$ at $x=0.2, 0.4$
8. Solve the equation $u_{xx} + u_{yy} = -81xy$, $0 < x < 1, 0 < y < 1$, given that $u(0,y)=0$, $u(x,0)=0$, $u(1,y) = 100$, $u(x,1) = 100$ and $h = \frac{1}{3}$
9. From the following table, estimate the number of students who obtained marks between 40 and 45:
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|-------------------------|-------|-------|-------|-------|-------|
| Marks: | 30-40 | 40-50 | 50-60 | 60-70 | 70-80 |
| No. of Students: | 31 | 42 | 51 | 35 | 31 |